

NAME: _____

DATE: _____

Hardy-Weinberg Practice Problems

1. At a locus with a dominant and recessive allele in a population that is in Hardy-Weinberg equilibrium, 16% of the individuals are homozygous for the recessive allele.

- a) What is the frequency of the dominant allele?
Since $q = 0.4$ & $p+q = 1$, $p + 0.4 = 1$, $p = 0.6$
- b) What is the frequency of the recessive allele?
Given: $q^2 = 0.16$, so $q = 0.4$
- c) What proportion of the population will show the dominant phenotype?
 $1 - 0.16 = 0.84$ OR $f(AA) + f(Aa) = (0.6)^2 + 2(0.6)(0.4) = 0.36 + 0.48 = 0.84$
- d) What proportion of the population will show the recessive phenotype?
**Since $q = 0.4$, $f(aa) = q^2 = (0.4)^2 = 0.16$
Alternatively, the $f(\text{recessive phenotype}) = f(\text{homozygous recessive genotype}) = 0.16$
given in the problem.**
- e) What proportion of the population will have the homozygous dominant genotype?
Since $p = 0.6$, $f(AA) = p^2 = (0.6)^2 = 0.36$
- f) What proportion of the population will be heterozygous?
Since $p = 0.6$ & $q = 0.4$, $f(Aa) = 2pq = 2(0.6)(0.4) = 0.48$
- g) What proportion of the population will have the homozygous recessive genotype?
**Given in the problem $f(aa) = 0.16$
Since $q = 0.4$, $f(aa) = q^2 = (0.4)^2 = 0.16$**

2. 25% of a population in Hardy-Weinberg equilibrium has a recessive-based disease. To have the disease, an individual must have both copies of the recessive allele.

- a) What is the frequency of the recessive allele?
Given in the problem $f(aa) = 0.25$, so $q^2 = 0.25$ $q = 0.5$
- b) What is the frequency of the dominant allele?
Since $q = 0.5$ & $p+q = 1$, $p + 0.5 = 1$, $p = 0.5$
- c) What proportion of the population will show the dominant phenotype?
 **$f(\text{dominant phenotype}) + f(\text{recessive phenotype}) = 1$
 $f(\text{dominant phenotype}) + 0.25 = 1$ $f(\text{dominant phenotype}) = 0.75$**
- d) What proportion of the population will show the recessive phenotype?
Given in the problem = 0.25
- e) What proportion of the population will have the homozygous dominant genotype?
Since $p = 0.5$, $f(AA) = p^2 = (0.5)^2 = 0.25$
- f) What proportion of the population will be heterozygous?
Since $p = 0.5$ & $q = 0.5$, $f(Aa) = 2pq = 2(0.5)(0.5) = 0.50$
- g) What proportion of the population will have the homozygous recessive genotype?
**Given in the problem $f(aa) = 0.25$
Since $q = 0.5$, $f(aa) = q^2 = (0.5)^2 = 0.25$**

3. 51% of a population in Hardy-Weinberg equilibrium is normal for the recessive-based disease, 3TC.

$$\begin{aligned} f(AA) + f(Aa) + f(aa) &= 1 & \& \quad 51\% = f(AA) + f(Aa), \text{ so } f(aa) = 0.49 \\ f(aa) = q^2 &= 0.49, & \quad q &= f(a) = 0.7 \\ p + q &= 1 & \quad p + 0.7 &= 1 & \quad p &= 0.3 \end{aligned}$$

- What percentage of the population is heterozygous for this trait?
 $f(Aa) = 2pq = 2(0.3)(0.7) = 0.42$
- What percentage of the population shows the recessive phenotype?
Since $q = 0.7$, $f(aa) = q^2 = (0.7)^2 = 0.49$
Given in the problem: $f(aa) = 1 - 0.51 = 0.49$
- What is the frequency of the dominant allele?
 $p = 0.3$ SEE ABOVE.

4. 4% of a population in Hardy-Weinberg equilibrium has phenylketonuria (PKU), a metabolic disorder that results from the homozygosity for a recessive allele.

- What is the frequency of the recessive allele?
 $f(aa) = q^2 = 0.04$, $q = f(a) = 0.2$
- What is the frequency of the dominant phenotype?
 $f(\text{dominant phenotype}) + f(\text{recessive phenotype}) = 1$
 $f(\text{dominant phenotype}) + 0.04 = 1$
 $f(\text{dominant phenotype}) = 0.96$
- What is the frequency of homozygote recessive in this population?
Given in the problem since $f(\text{recessive phenotype}) = f(\text{homozygous recessive genotype}) = 0.04$
- What is the frequency of homozygote dominant in this population?
If $q = 0.2$ & $p + q = 1$, $p = 0.8$
 $f(AA) = p^2 = (0.8)^2 = 0.64$

5. 91% of a feline population in Hardy-Weinberg equilibrium display polydactyly. Polydactyly is a dominant disease.

- What is the frequency of the recessive allele?
 $f(AA) + f(Aa) + f(aa) = 1$ & $f(AA) + f(Aa) = 0.91$
 $0.91 + f(aa) = 1$ $f(aa) = 0.09$
 $f(aa) = q^2 = 0.09$, $q = f(a) = 0.3$
- What is the frequency of felines with the homozygous recessive genotype?
 $f(aa) = q^2 = 0.09$ SEE ABOVE FOR FURTHER EXPLANATION
- What is the frequency of felines who do not display polydactyly?
 $f(aa) = q^2 = 0.09$ SEE ABOVE FOR FURTHER EXPLANATION

6. A population in Hardy-Weinberg has an allelic frequency of the recessive allele of 0.20.

- What is the frequency of the dominant allele?
GIVEN: $q = 0.20$ & $p + q = 1$, $p + 0.2 = 1$ $p = 0.8$
- What is the frequency of the heterozygote genotype in this population?
 $p = 0.8$ & $q = 0.2$, $f(Aa) = 2(p)(q) = 2(0.8)(0.2) = 0.32$
- What proportion of the population display the dominant phenotype?
 $f(AA) + f(Aa) + f(aa) = 1$ & $q = 0.2$ $q^2 = f(aa) = 0.04$
 $f(AA) + f(Aa) + 0.04 = 1$
 $f(AA) + f(Aa) = 0.96$